

COMP371

COMPUTER GRAPHICS

LECTURE 10

LIGHTING AND SHADING

Lecture Overview

- Review of last class
- Global and Local Illumination
- Normal Vectors
- Light Sources
- Phong Illumination Model

Global Illumination

- Ray tracing
- Radiosity
- Photon Mapping
- Follow light rays through a scene
- Accurate, but expensive (off-line)



Tobias R. Metoc

Raytracing example

Martin Moeck,
Siemens Lighting



Radiosity Example

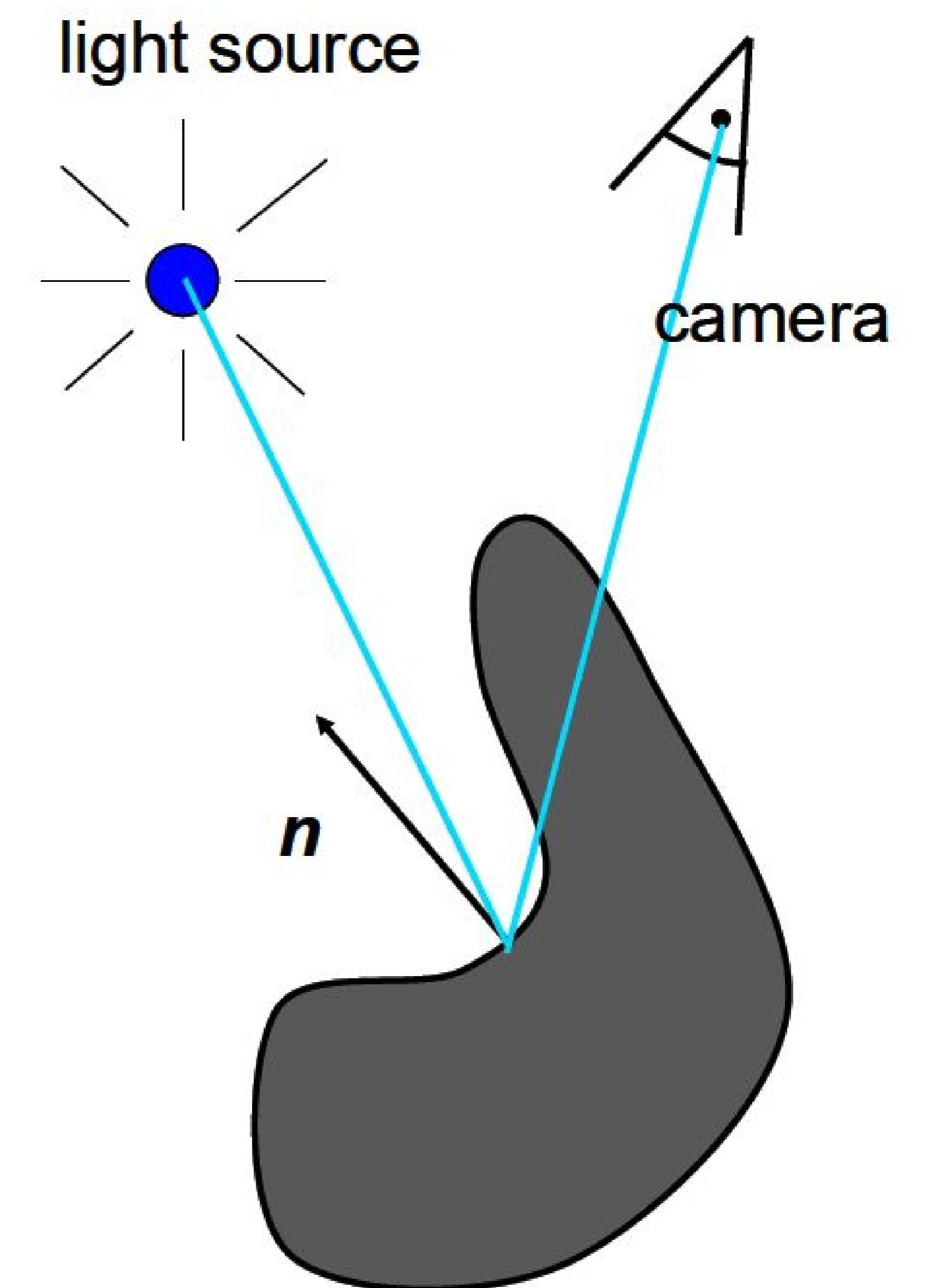
Restaurant Interior.

Guillermo Leal, Evolucion Visual



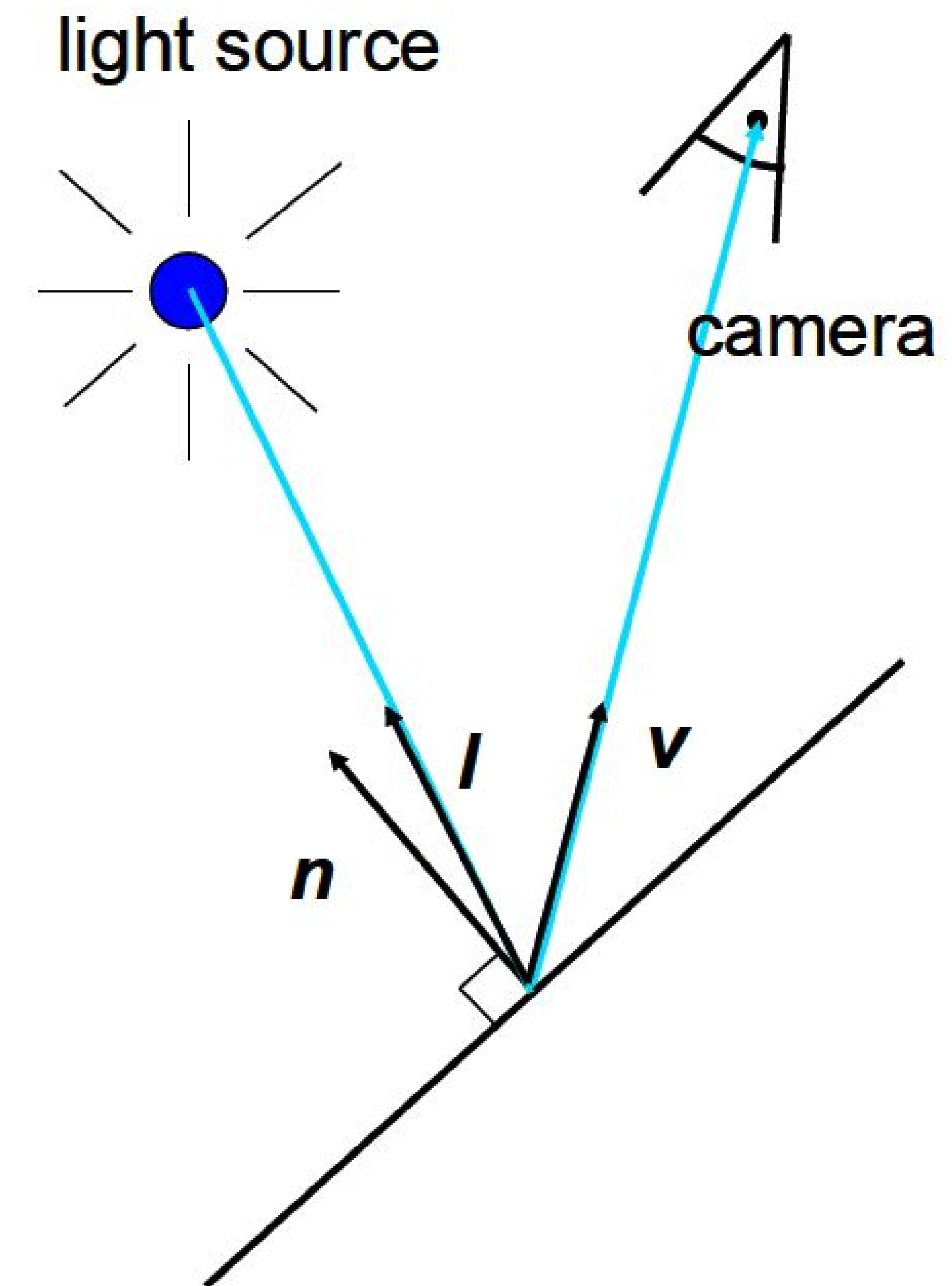
Local Illumination

- Approximate model
- Local interaction between light, surface, viewer
- Phong model (this lecture):
 - fast, supported in OpenGL
- GPU shaders



Local Illumination cont'd

- Color determined only based on surface normal, relative camera position and relative light position
- What effects does this ignore?



Normal Vectors

- Must calculate and specify the normal vector
 - Even in OpenGL!

- Example: plane

Method 1: Normal of a plane

- Method 1: given by $f(p) = ax + by + cz + d = 0$
- Let p_0 be a known point on the plane
- Let p be an arbitrary point on the plane
- Recall: $u \cdot v = 0$ if and only if u orthogonal to v
- $n \cdot (p - p_0) = n \cdot p - n \cdot p_0 = 0$
- Consequently $n_0 = [a \ b \ c]^T$
- Normalize to $n = n_0/|n_0|$

Method 2: Normal of a plane

- Method II: plane given by p_0, p_1, p_2
- Points must not be collinear \rightarrow cross product defined as 0
- Recall: $u \times v$ orthogonal to u and v
- $n_0 = (p_1 - p_0) \times (p_2 - p_0)$
- Order of cross product determines orientation
- Normalize to $n = n_0/|n_0|$

Reflected Vector

- Perfect reflection: angle of incidence equals angle of reflection
- Also: l , n , and r lie in the same plane \rightarrow
- Assume $|l| = |n| = 1$, guarantee $|r| = 1$

$$l \cdot n = \cos\theta = n \cdot r$$

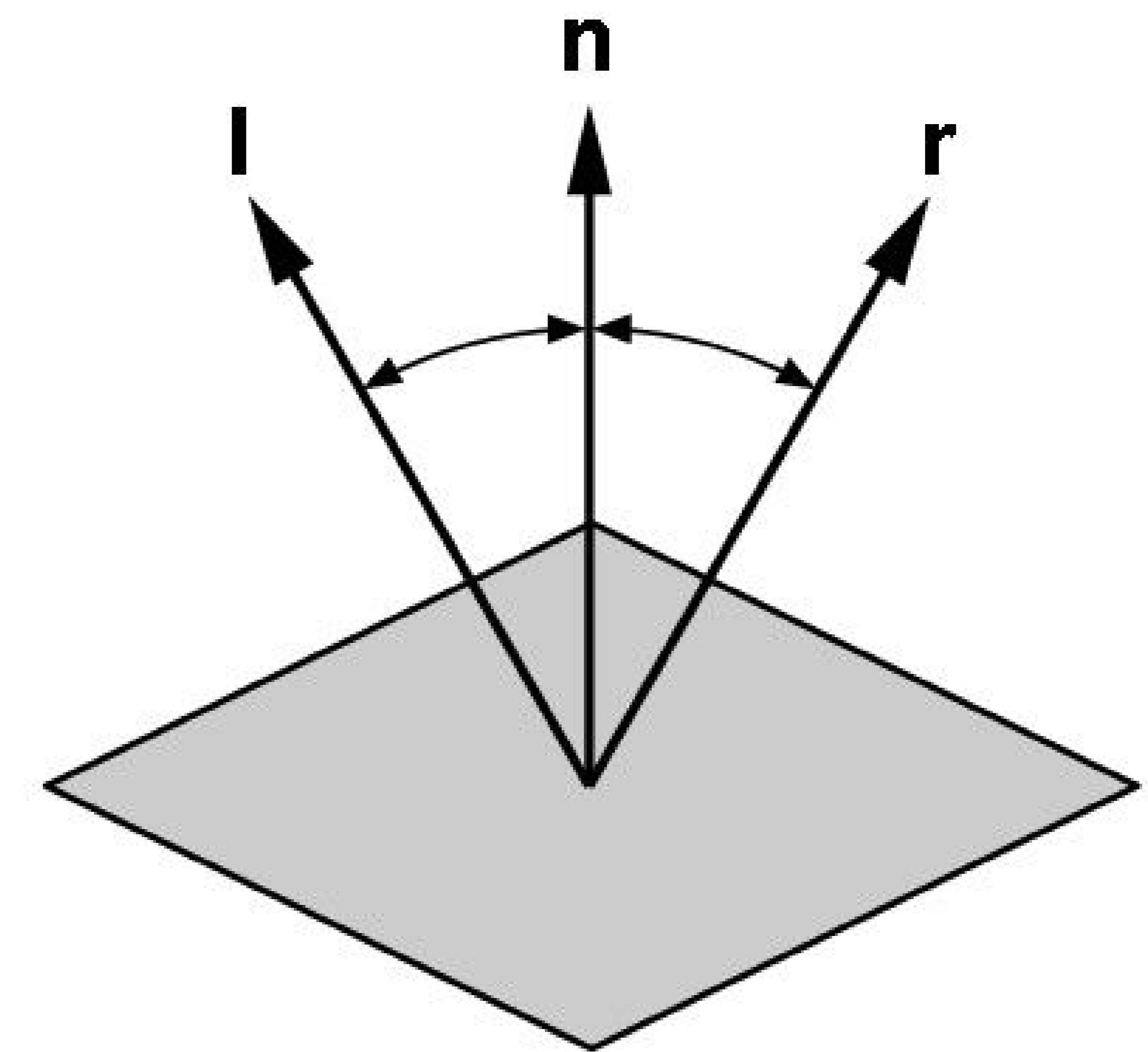
$$r = al + bn$$

Can write r as a linear combination of l and n

$$(1) n \cdot r = al \cdot n + b = l \cdot n$$

$$(2) 1 = r \cdot r = a^2 + 2ab l \cdot n + b^2$$

$$\text{Solution: } a = -1 \text{ and } b = 2(l \cdot n) \rightarrow r = 2(l \cdot n)n - l$$



Light Sources and Material Properties

- Appearance depends on
 - Light sources, their locations and properties
 - Material (surface) properties
 - Viewer position

Types of Light Sources

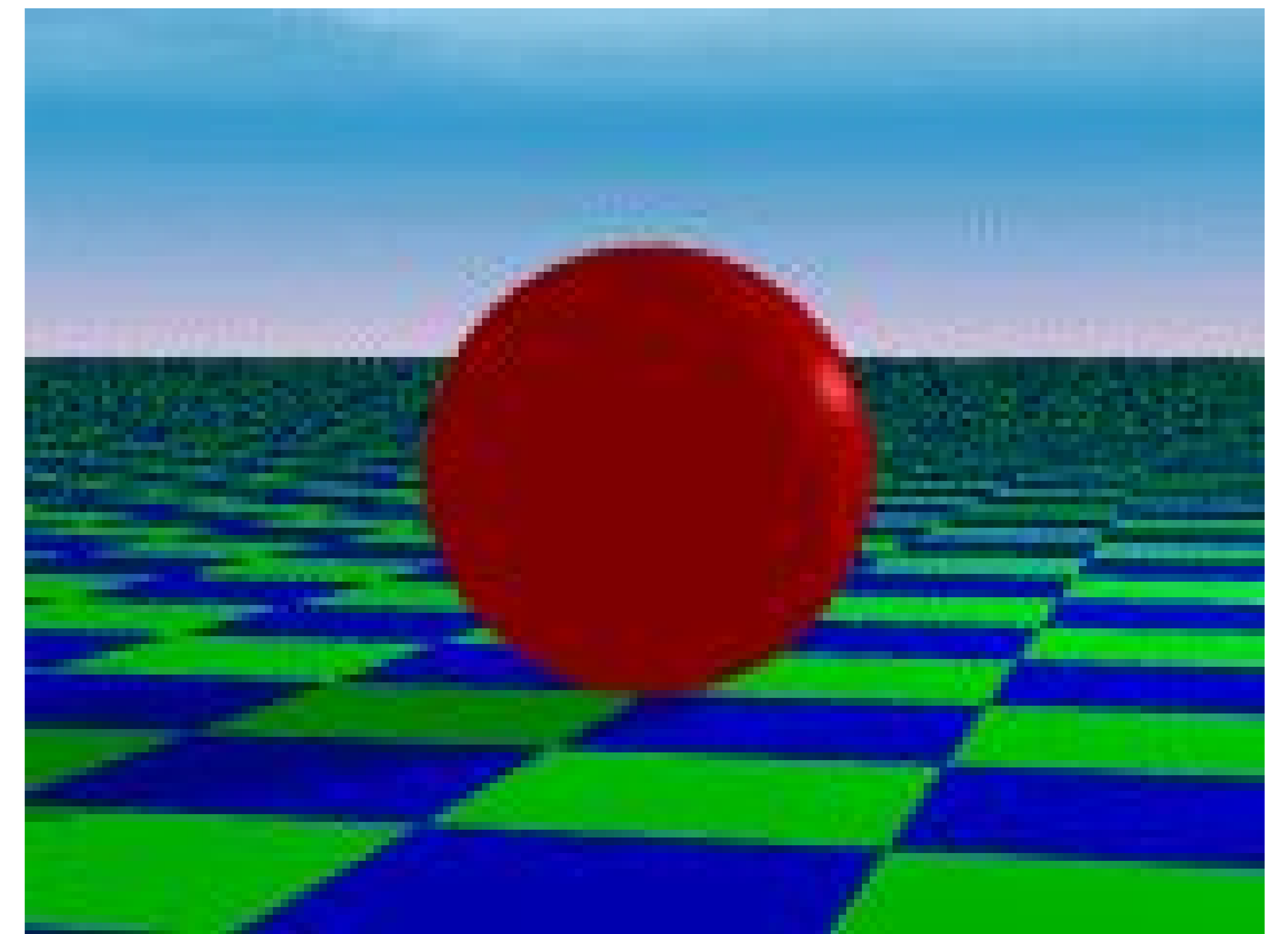
- Ambient light: no identifiable source or direction
- Point source: given only by point
- Directional light: given only by direction
- Spotlight: from source in direction
 - Cut-off angle defines a cone of light
 - Attenuation function (brighter in center)



Point Source

- Given by a point p_0
- Light emitted equally in all directions
- Intensity decreases with square of distance

$$I \propto \frac{1}{|p - p_0|^2}$$

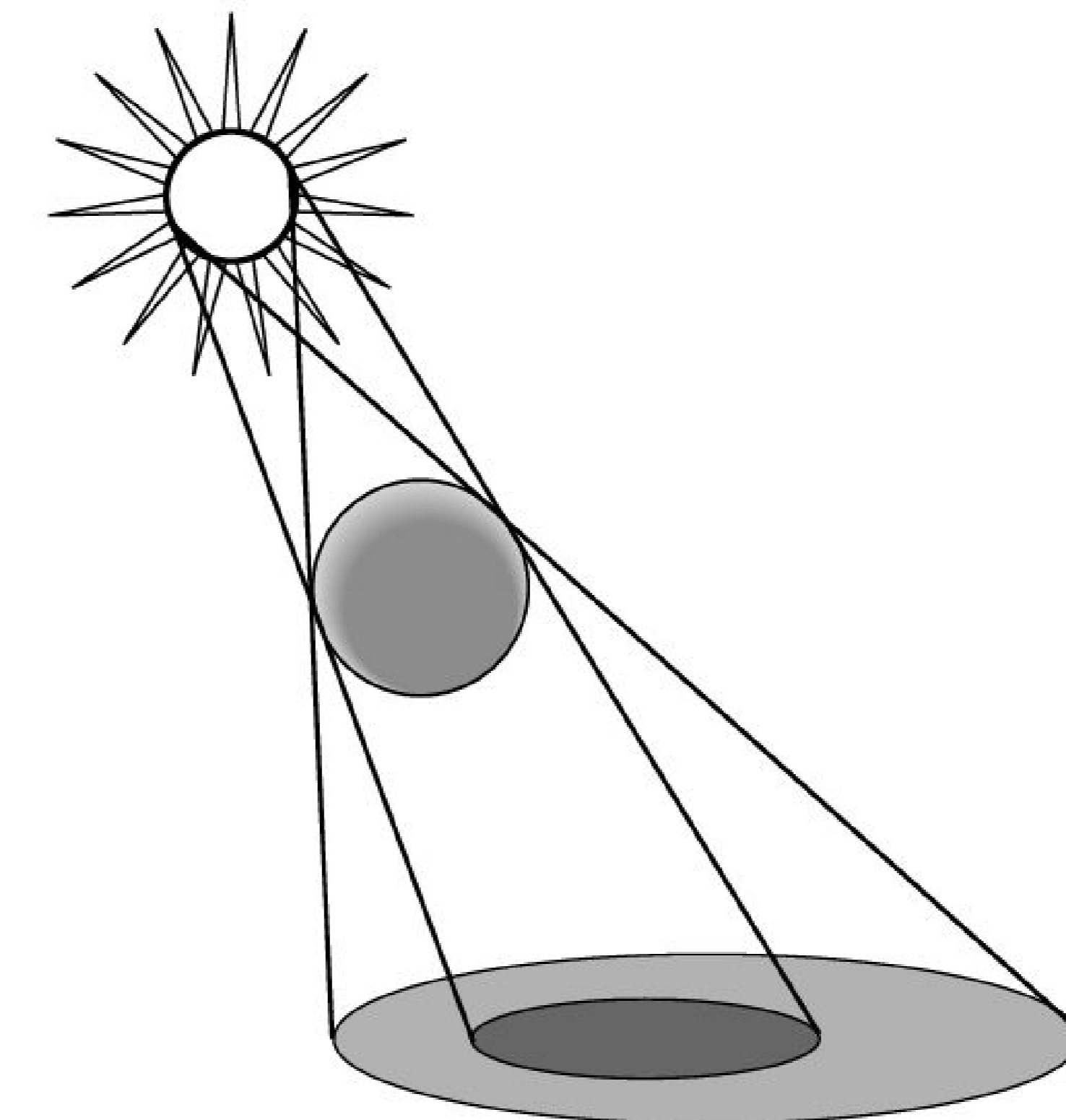


Limitations of Point Sources

- Shading and shadows inaccurate
- Example: penumbra (partial “soft” shadow)
- Similar problems with highlights
- Compensate with attenuation
- Softens lighting
- Better with ray tracing
- Better with radiosity

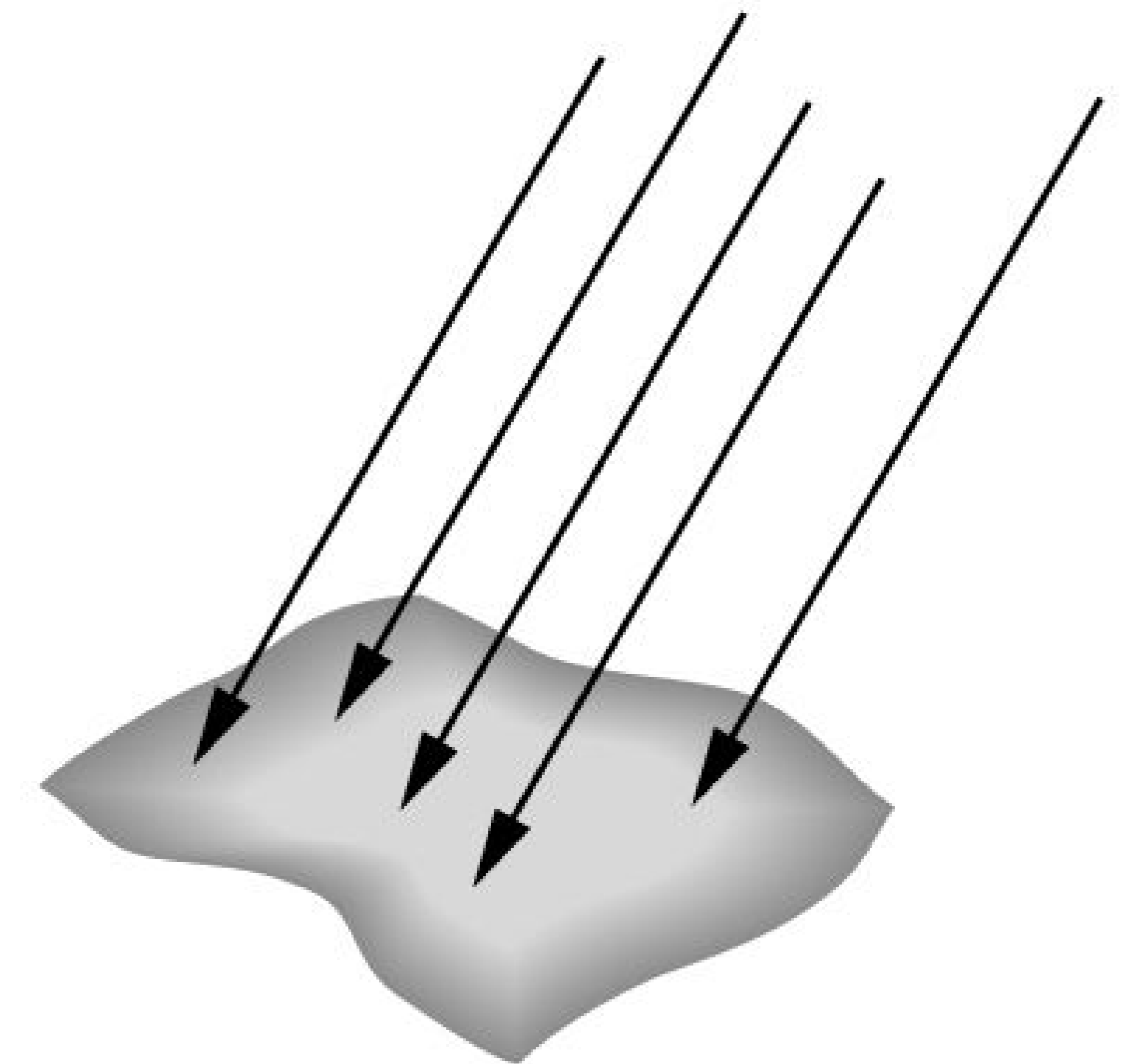
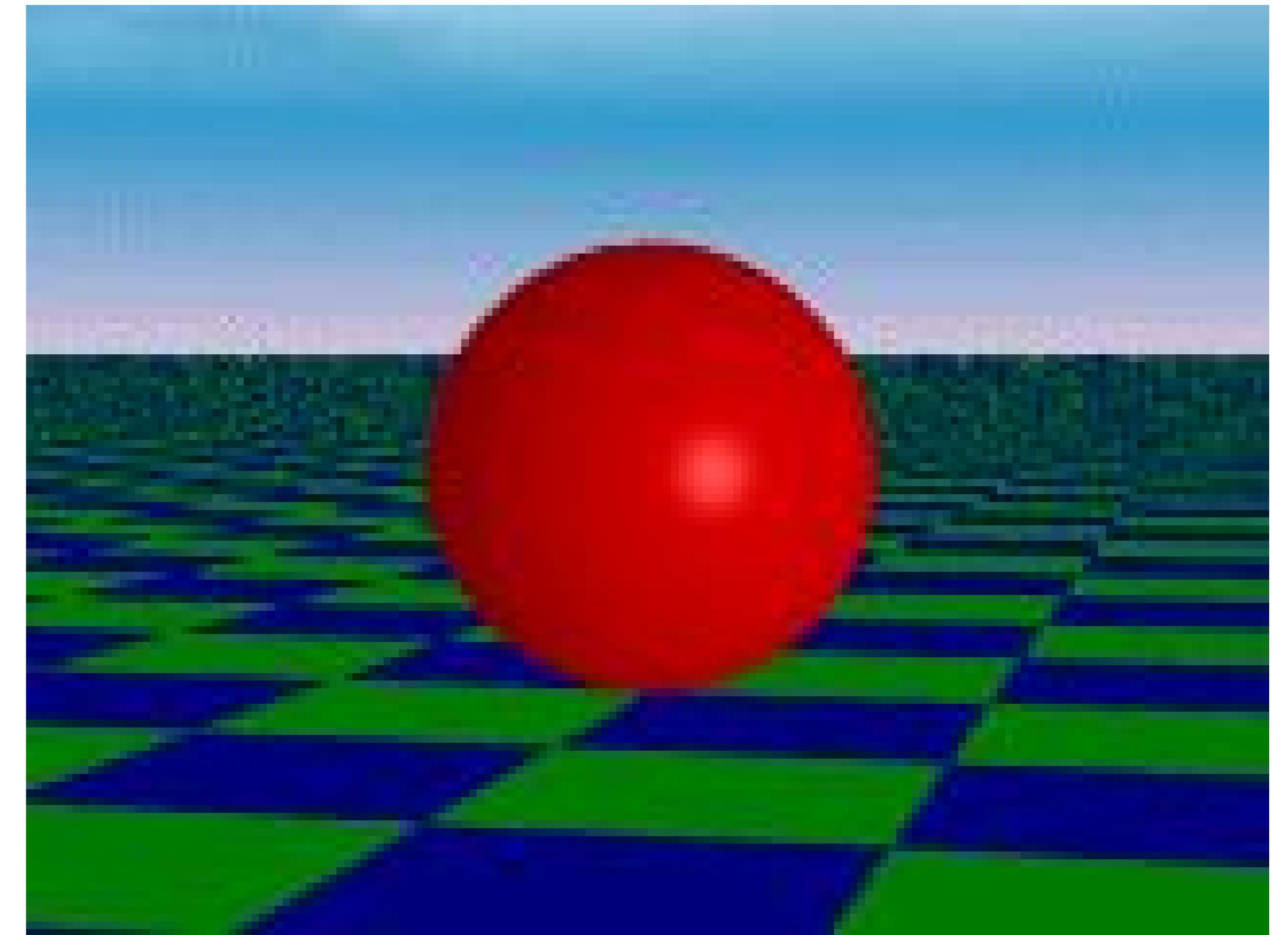
$$\frac{1}{a + bq + cq^2}$$

$q = \text{distance } |p - p_0|$
 $a, b, c \text{ constants}$



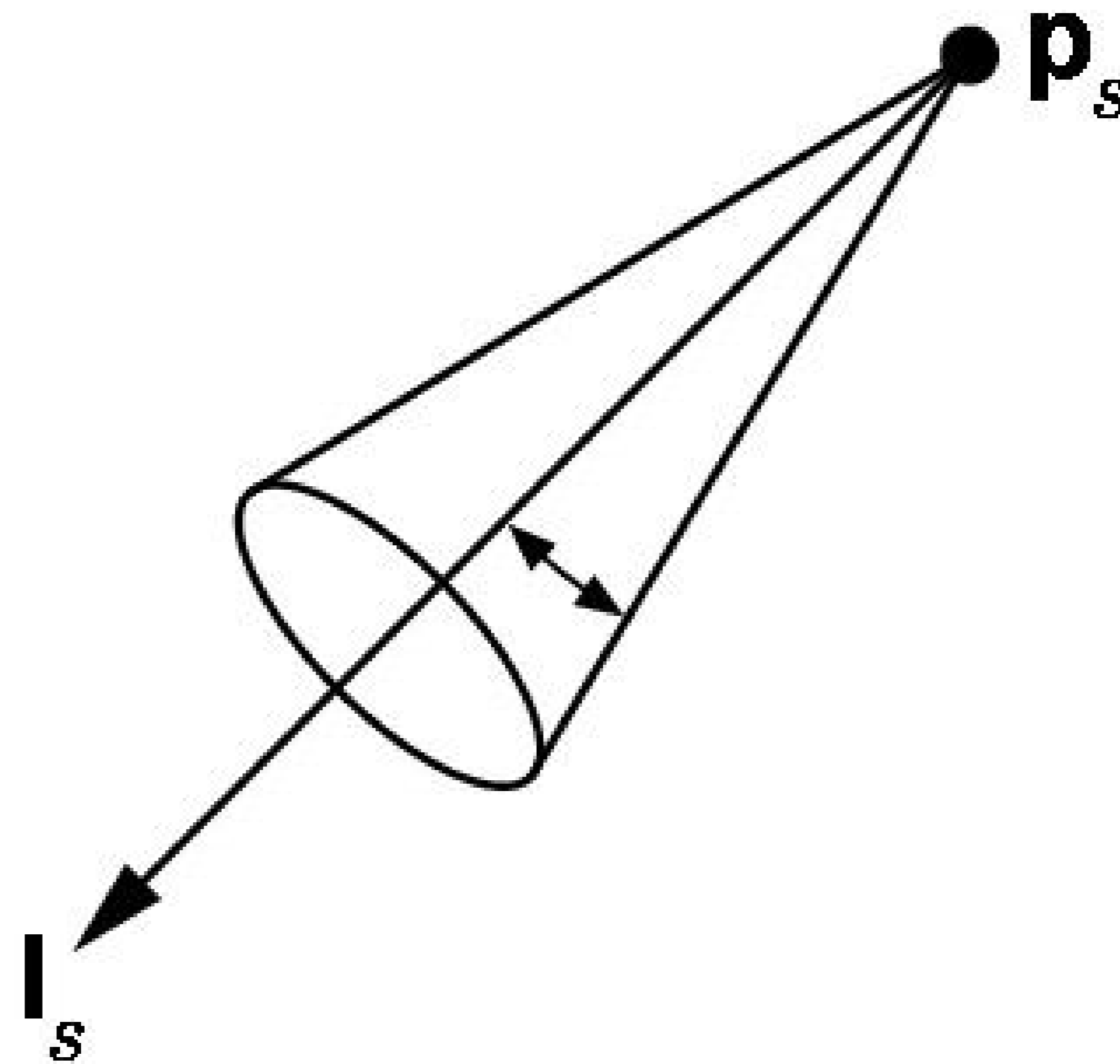
Directional Light Source

- Given by a direction vector
- Simplifies some calculations
- In OpenGL:
 - Point source $[x \ y \ z \ 1]^T$
 - Directional source $[x \ y \ z \ 0]^T$



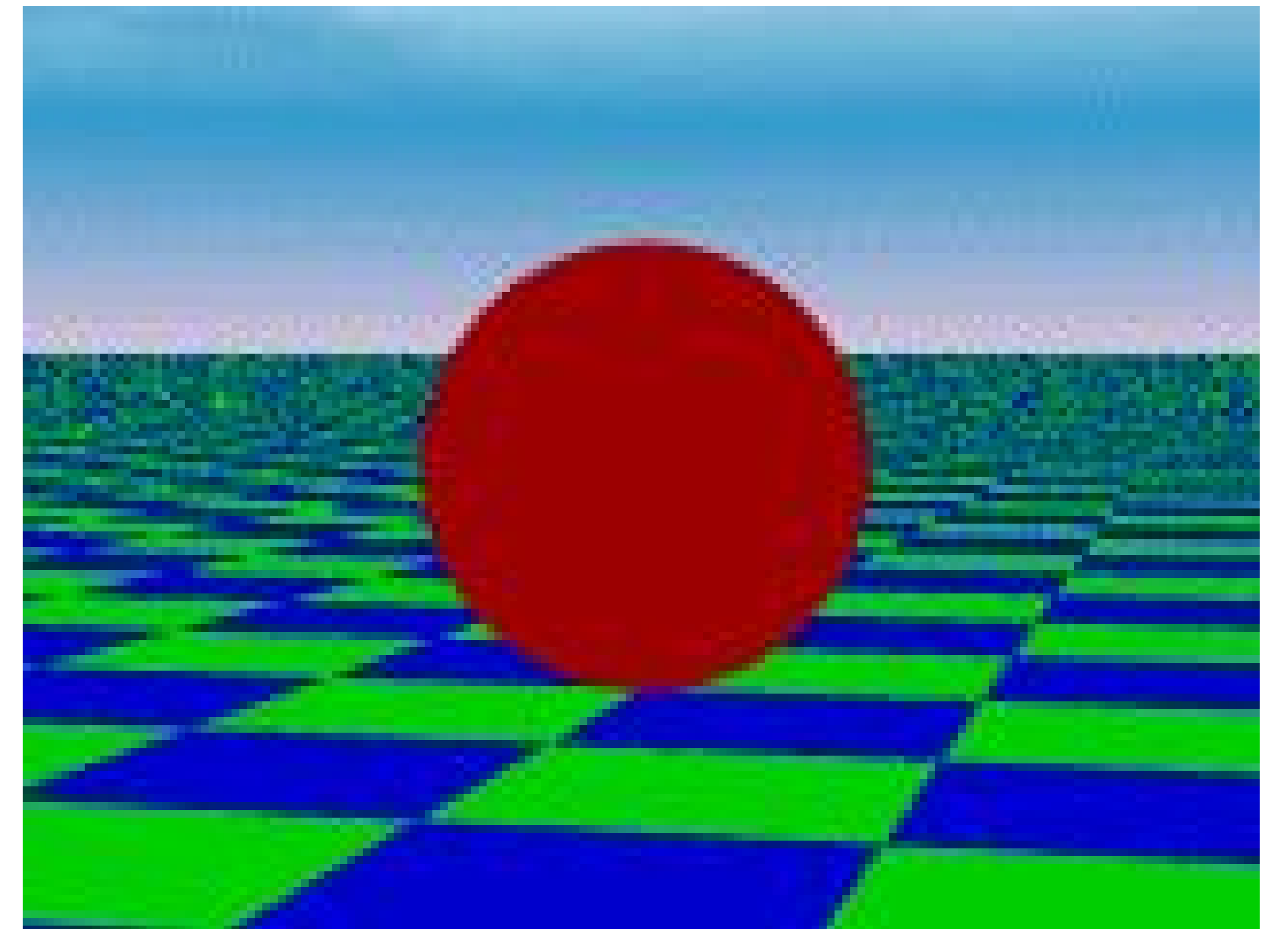
Spotlight

- Most complex light source in OpenGL
- Light still emanates from point
- Cut-off by cone determined by angle θ



Global Ambient Light

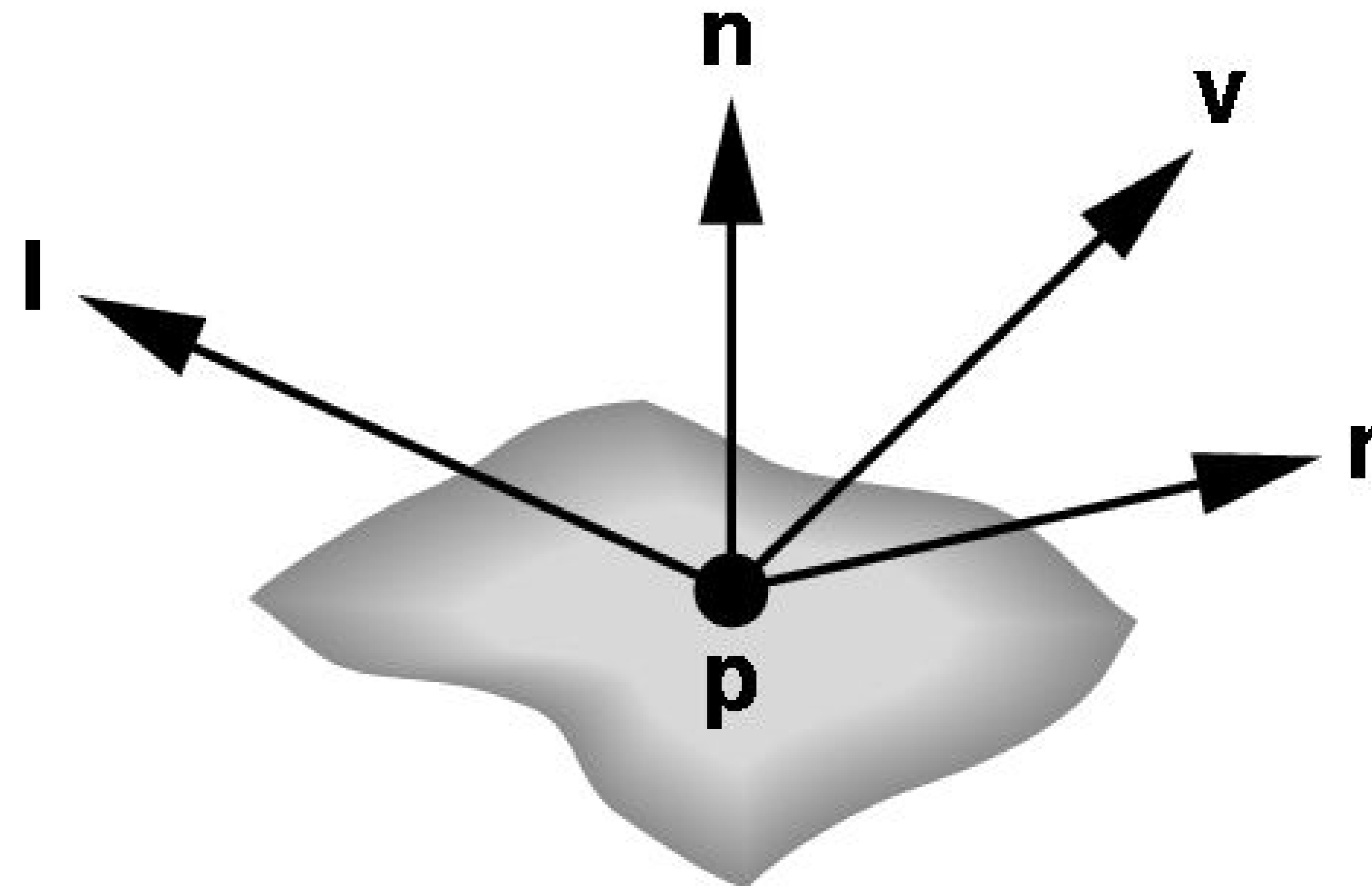
- Independent of light source
- Lights entire scene
- Computationally inexpensive
- Simply add $[G_R \ G_G \ G_B]$ to every pixel on every object
- Not very interesting on its own.
 - A cheap hack to make the scene brighter.



Phong Illumination Model

- Calculate color for arbitrary point on surface
- Compromise between realism and efficiency
- Local computation (no visibility calculations)
- Basic inputs are material properties and I , n , v :

I = unit vector to light source
 n = surface normal
 v = unit vector to viewer
 r = reflection of I at p
(determined by I and n)



Phong Illumination Overview

1. Start with global ambient light $[G_R \ G_G \ G_B]$
 2. Add contributions from each light source
 3. Clamp the final result to $[0, 1]$
- Calculate each color channel (R,G,B) separately
 - Light source contributions decomposed into
 - Ambient reflection
 - Diffuse reflection
 - Specular reflection
 - Based on ambient, diffuse, and specular *lighting and material* properties

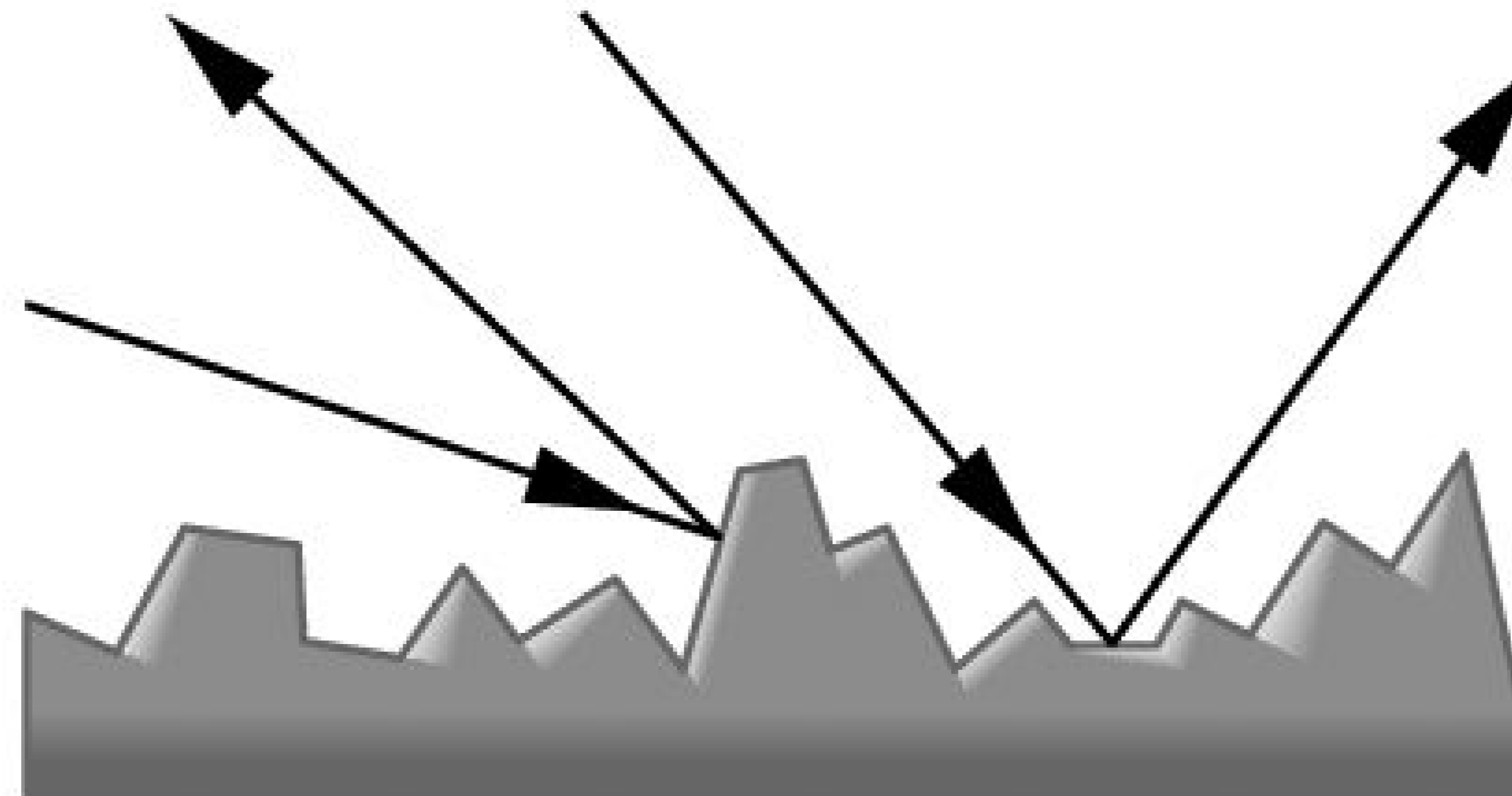
Ambient Reflection

$$I_a = k_a L_a$$

- Intensity of ambient light is uniform at every point
- Ambient reflection coefficient k_a , $0 \leq k_a \leq 1$
- May be different for every surface and r,g,b
- Determines reflected fraction of ambient light
- L_a = ambient component of light source (can be set to different value for each light source)
- Note: L_a is not a physically meaningful quantity

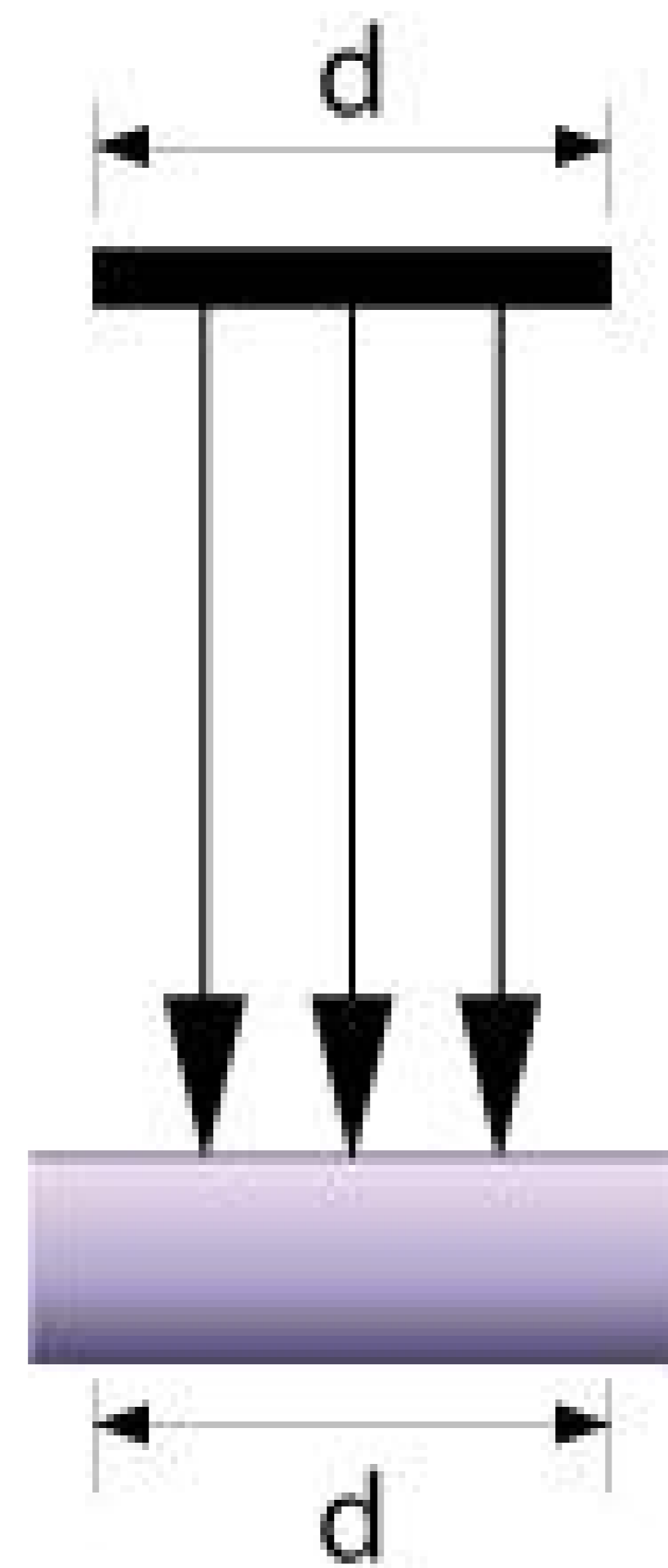
Diffuse Reflection

- Diffuse reflector scatters light equally to all directions
- Called *Lambertian* surface
- Diffuse reflection coefficient k_d , $0 \leq k_d \leq 1$
- Only the angle of incoming light is important

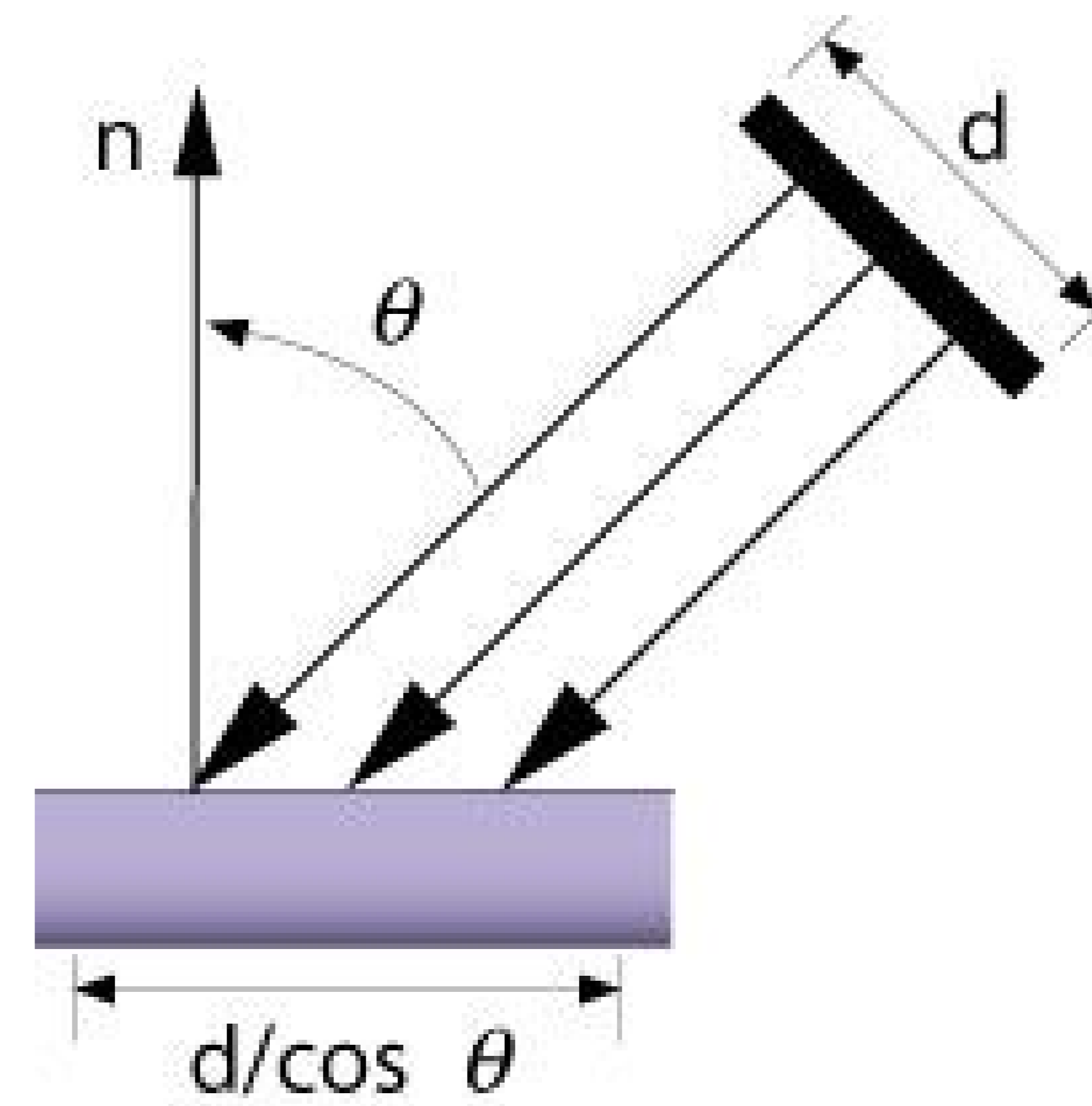


Lambert's Law

Intensity depends on angle of incoming light



(a)



(b)

Diffuse Light Intensity Depends on Angle of Incoming Light

• Recall

l = unit vector to light

n = unit surface normal

θ = angle to normal

- $\cos \theta = l \cdot n$

- $I_d = k_d L_d (l \cdot n)$

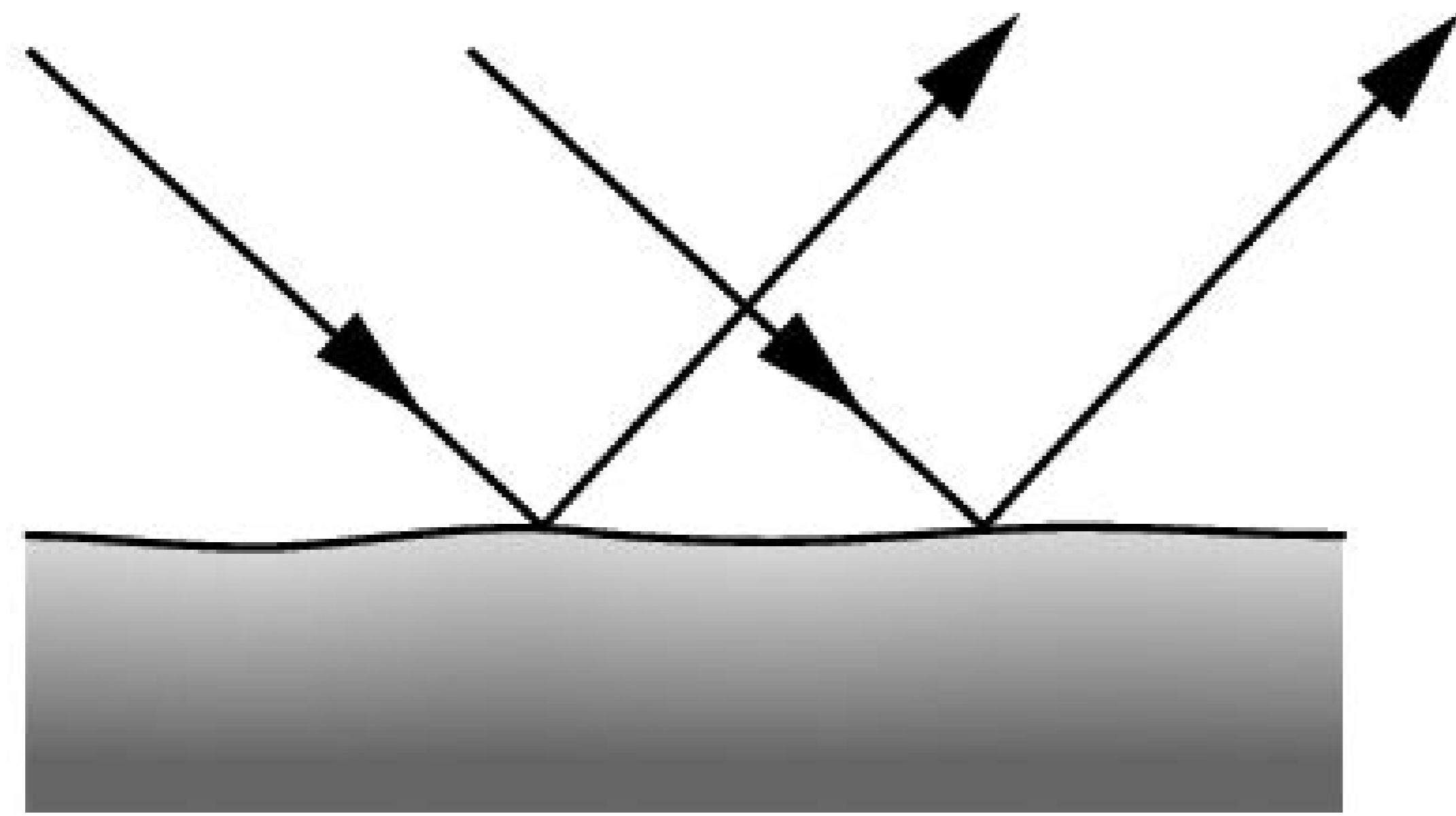
- With attenuation:
$$I_d = \frac{k_d L_d}{a + bq + cq^2} (l \cdot n)$$

q = distance to light source,

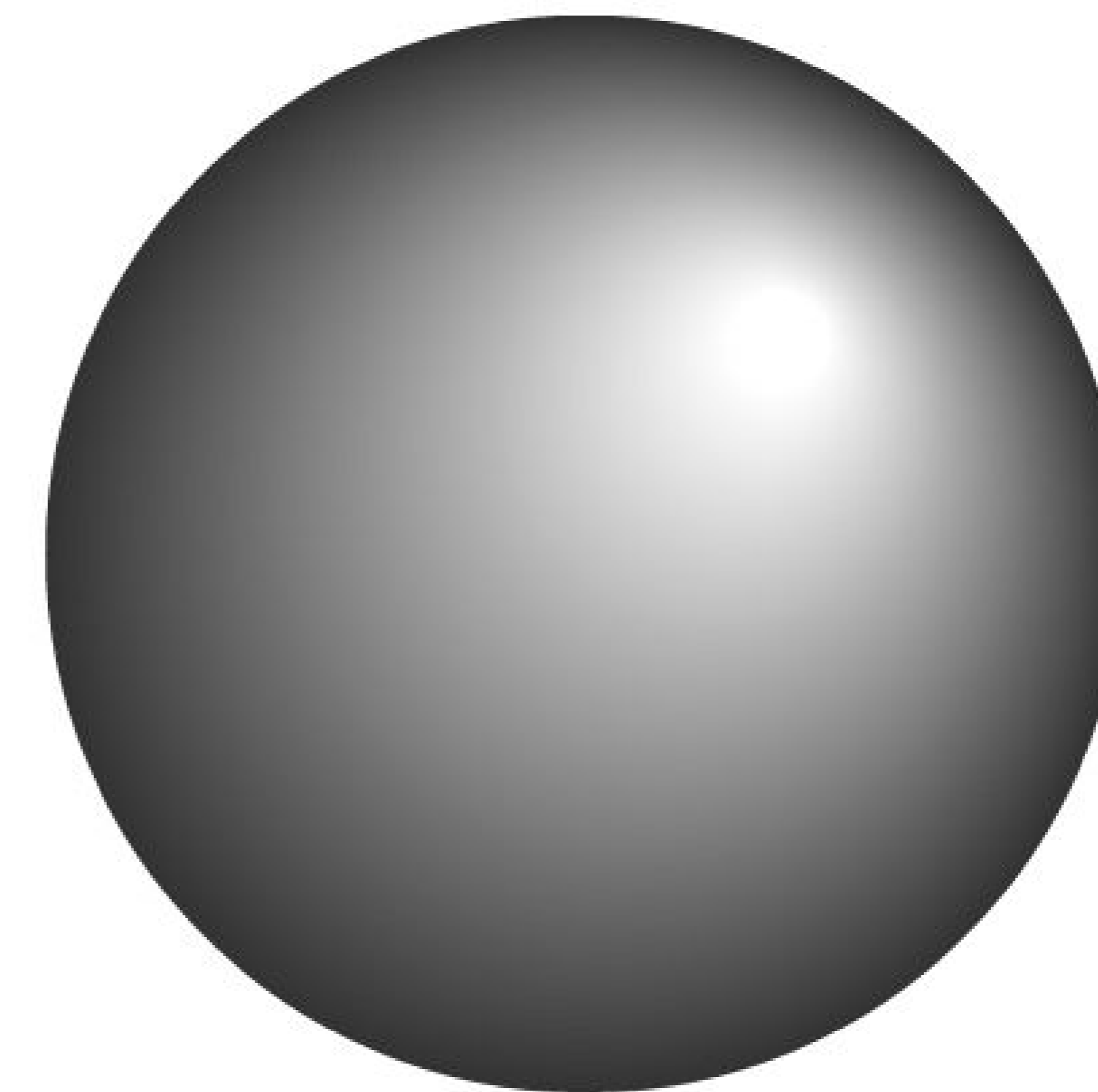
L_d = diffuse component of light

Specular Reflection

- Specular reflection coefficient k_s , $0 \leq k_s \leq 1$
- Shiny surfaces have high specular coefficient
- Used to model specular highlights
- Does not give mirror effect (need other techniques)



Specular reflection



Specular highlights

Specular Reflection

- Recall

- v = unit vector to camera

- r = unit reflected vector

- φ = angle between v and r

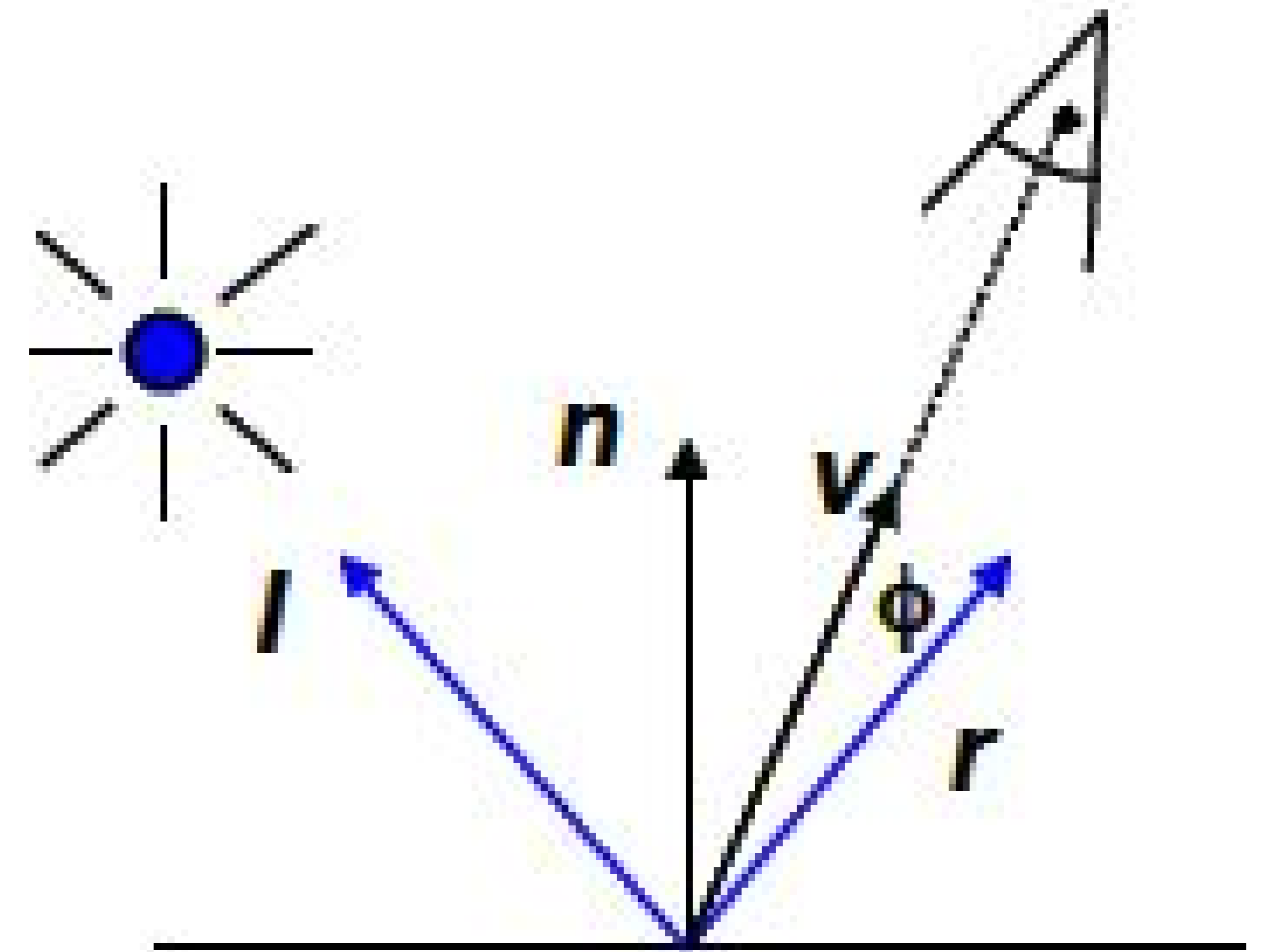
- $\cos \varphi = v \cdot r$

- $I_s = k_s L_s (\cos \varphi)^\alpha$

- L_s is specular component of light

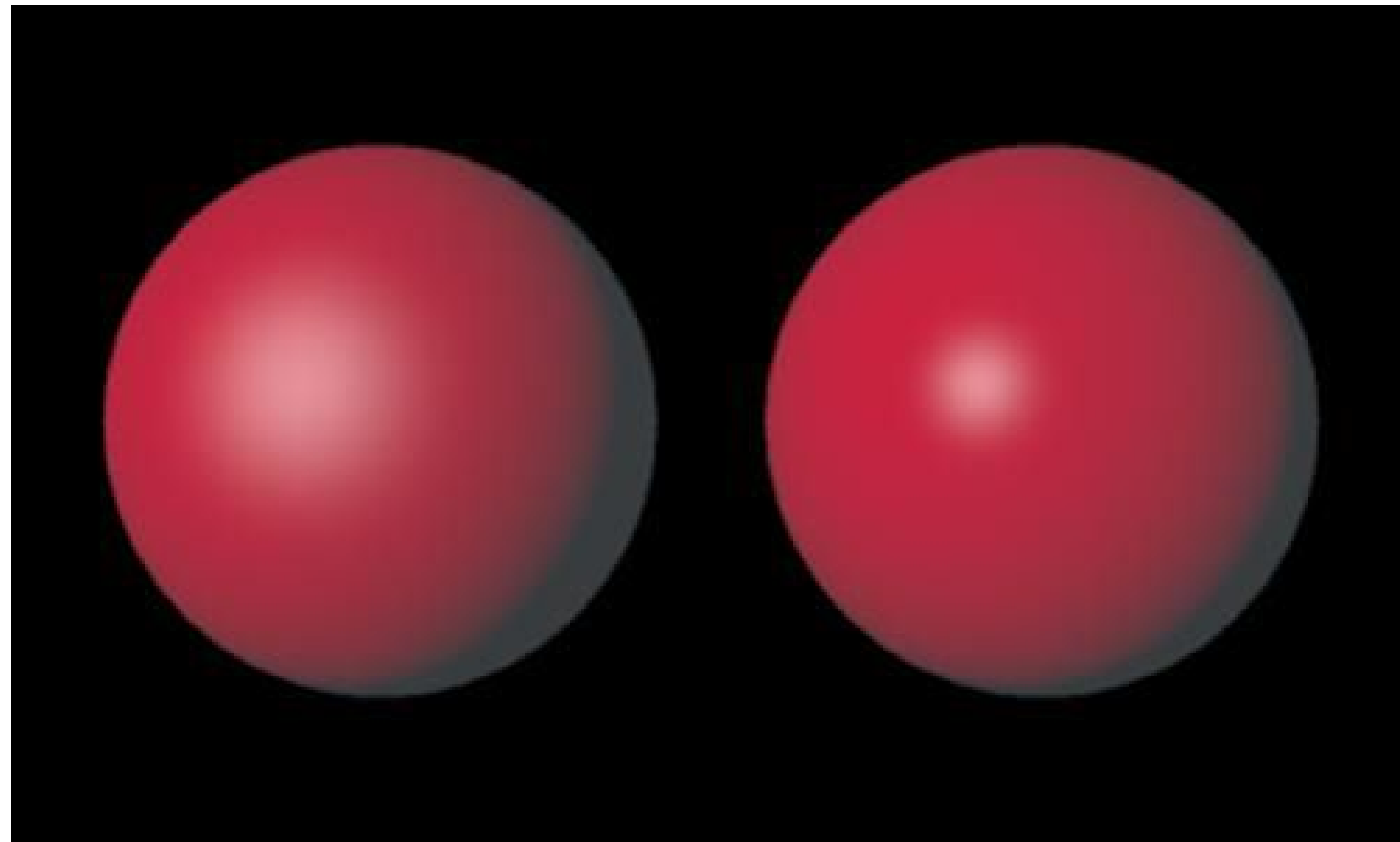
- α is shininess coefficient

- Can add distance term as well



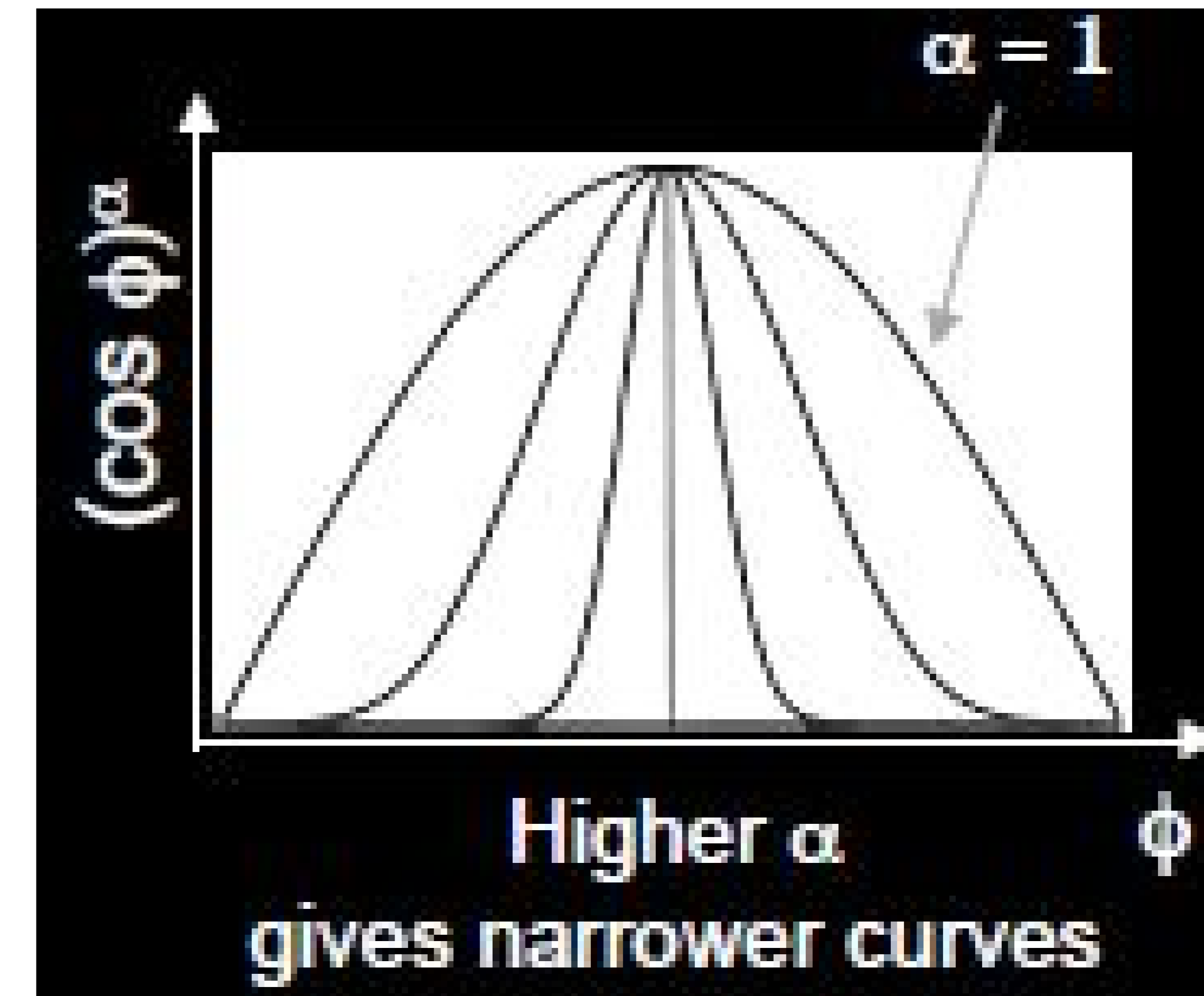
Shininess Coefficient

- $I_s = k_s L_s (\cos \phi)^\alpha$
- α is the shininess coefficient



low α

high α



Summary of Phong Model

- Light components for each color:
 - Ambient (L_a), diffuse (L_d), specular (L_s)
- Material coefficients for each color:
 - Ambient (k_a), diffuse (k_d), specular (k_s)
- Distance q for surface point from light source

l = unit vector to light

n = surface normal

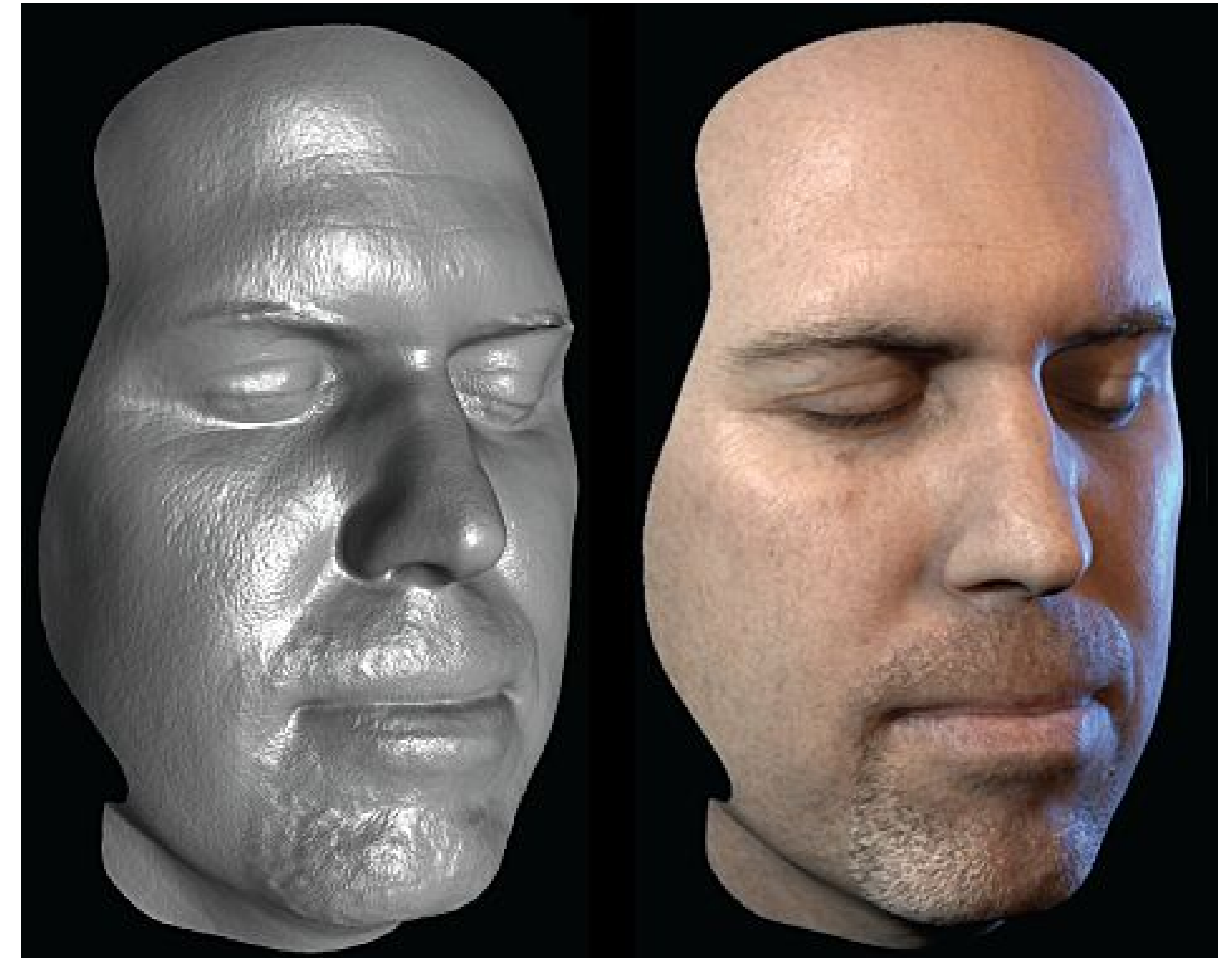
r = l reflected about n

v = vector to viewer

$$I = \frac{1}{a + bq + cq^2} (k_d L_d (l \cdot n) + k_s L_s (r \cdot v)^\alpha) + k_a L_a$$

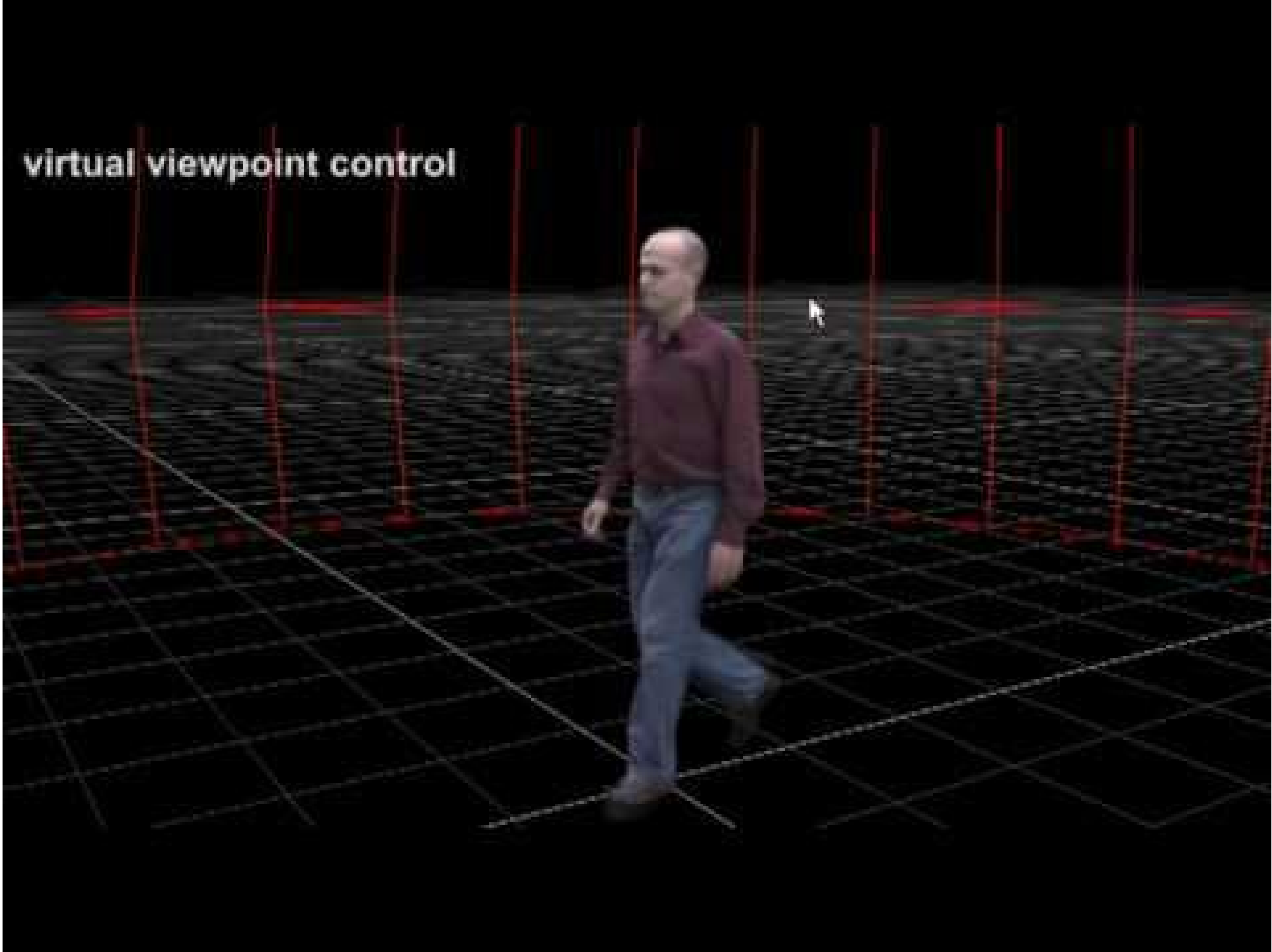
BRDF

- Bidirectional Reflection Distribution Function
- Must measure for real materials
- Isotropic vs. anisotropic
- Mathematically complex
- Programmable pixel shading



Lighting properties of a human face were captured and face re-rendered;
Institute for Creative Technologies

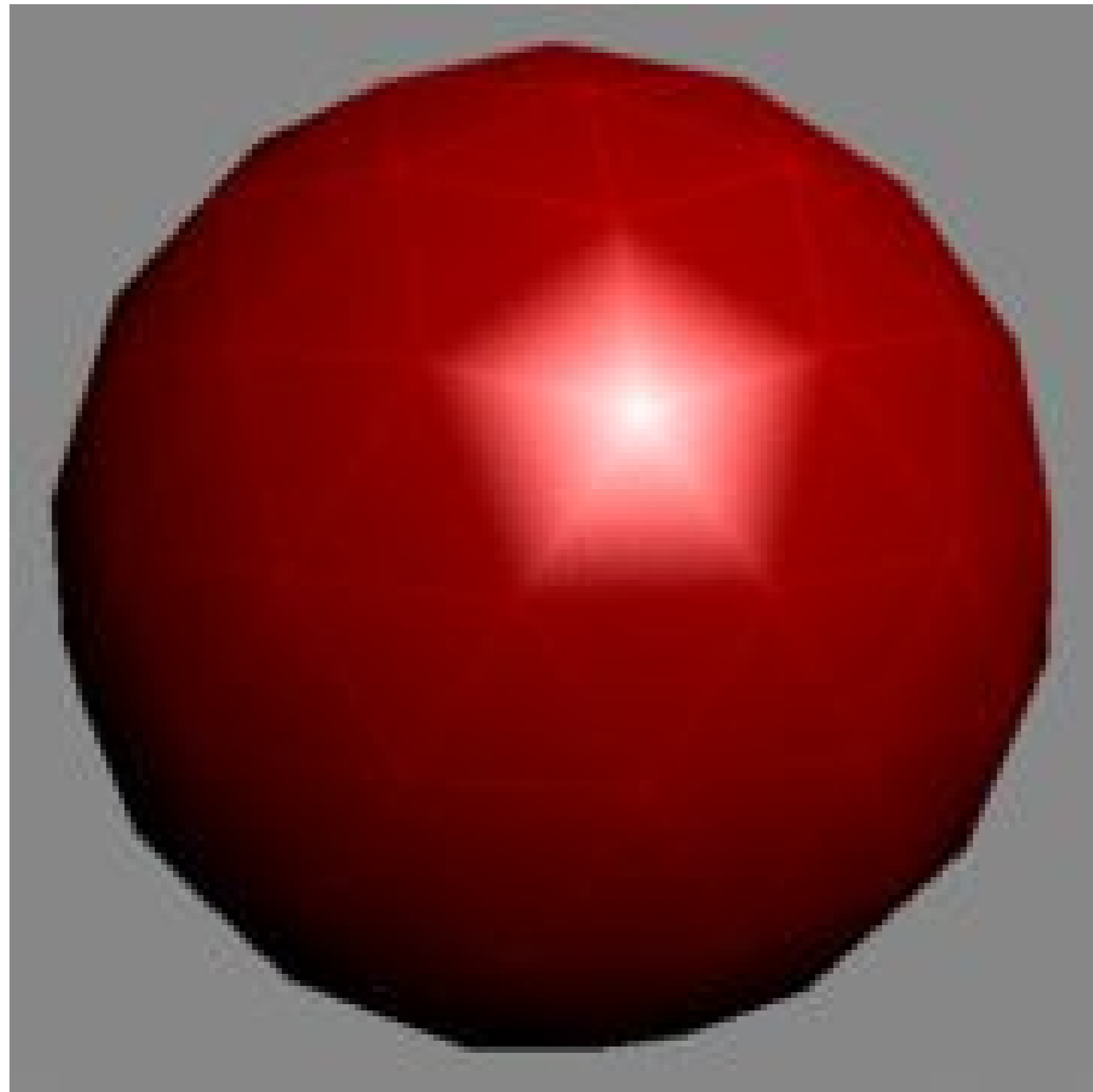
virtual viewpoint control



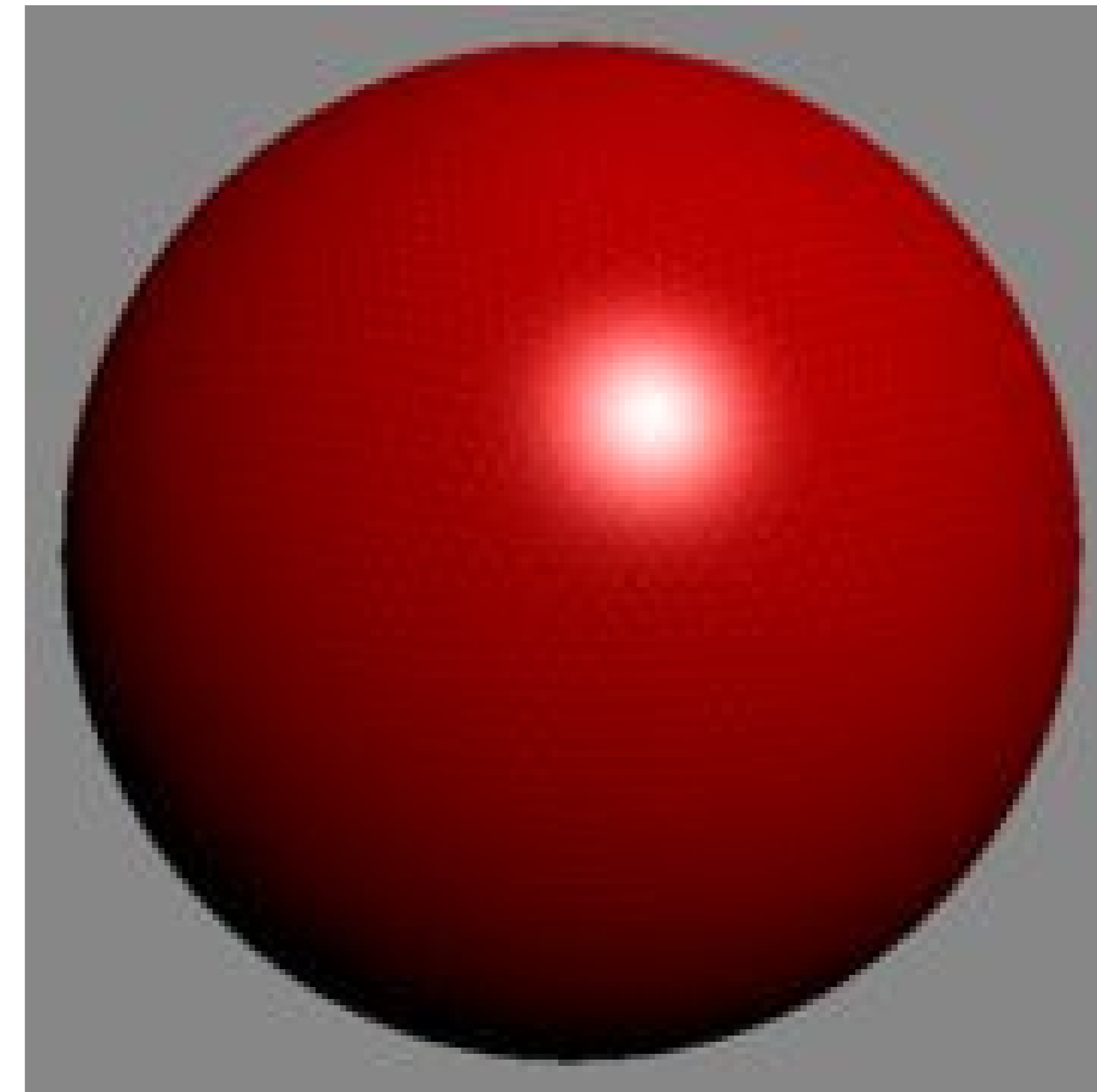
Gouraud Shading

- “Fixed Pipeline” OpenGL implements Gouraud Shading
- Gouraud Shading is an implementation of the Phong Shading Model where Lighting is computed per-vertex
- The result is then interpolated on the whole Triangle
- Specular highlights are typically blurry, a high tessellation is required for good lighting
- It can be completely implemented in a Vertex Shader

Gouraud Shading



Low Poly Count



High Poly Count

Phong Shading

- Is typically implemented per Fragment (pixel)
- It provides “sharp” specular highlights even with low polygon count since lighting is calculated for each pixel individually.
- It is implemented on both the Vertex and Fragment Shader
- The Vertex Shader Transforms the Lighting Data to View Space
- The Fragment Shader calculates the Phong Shading Equation (Ambient + Diffuse + Specular)

Phong Model Implementation with GLSL

- Light Properties and Material Properties are implemented as Shader Uniform Variables
- Be careful from which Coordinate System the Light Positions are sent to the Shaders
- Typically, lighting is computed in View Space
 - Normals must be converted
 - Eye, Light vectors must be converted

Phong Shading in GLSL

Vertex Shader

- Transform vertex positions to Clip Space
- Transform lighting data to View Space

Fragment Shader

- Calculate and add ambient, diffuse and specular components

Phong Shading in GLSL

- Vertex Shader
- Uniforms
 - Light position
 - Transformation Matrices
- Input
 - Vertex Data
(pos, normal, color)
- Output
 - Normal (N)
 - Light Vector (L)
 - Eye Vector (V)
 - Vertex Color
- Fragment Shader
- Uniforms
 - Material Coefficients
(ka, kd, ks, n)
 - Light Coefficients
(Color, Attenuation const)
- Inputs in View Space
 - Normal (N)
 - Light Vector (L)
 - Eye Vector (V)
- Output
 - Fragment Color

Phong Shading in GLSL Multiple Light Sources


- Use arrays for light parameters in your Shaders to support multiple light sources.

Review

- Global and Local Illumination
- Normal Vectors
- Light Sources
- Phong Illumination Model
- Gouraud and Phong Shading

Next Lecture

- OpenGL shading



CONCORDIA.CA

Studying Support Slides